

Optimal Model Complexity in Geological Carbon Sequestration: A Design of Experiment (DoE) & Response Surface (RS) Uncertainty Analysis

Project Number: DE-FE-0009238

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U.S. Department of Energy
National Energy Technology Laboratory
Carbon Storage R&D Project Review Meeting
Developing the Technologies and
Infrastructure for CCS
August 20-22, 2013

Presentation Outline

- Project major goals and benefits;
- Detailed project objectives & success criteria;
- Accomplishments to date;
- Summary of results;
- Appendix (organization chart; Gantt chart; additional results).

Benefit to the Program

Major goals:

Support industry's ability to predict CO₂ storage capacity in geologic formations to within $\pm 30\%$ accuracy; Develop and validate technologies to ensure 99% storage permanence.

Project benefits:

We will facilitate the development and implementation of efficient workflows for modeling field-scale geological carbon sequestration (GCS) in a variety of geochemically reactive environments, where subsurface formations exhibit multiple scales of permeability (k) heterogeneity.

Project Overview:

Specific Goals and Objectives

- Develop, test, and verify the DoE and RS uncertainty analysis for a fully heterogeneous reference model (FHM) & **increasingly lower resolution** “geologic models” created from upscaling the FHM. For all models:
 - (1) within the uncertainty framework over multiple time scales, identify influential parameters (and processes) on making various predictions and to quantify their prediction uncertainties: *pressure evolution, CO₂ footprint, CO₂ storage ratio, CO₂/brine leakage, distributions of geochemical species, and ϕ/k changes in the storage system (reservoir + caprock) and their feedback with flow modeling.*
 - (2) At increasing time scales, evaluate **optimal heterogeneity resolution(s)** by comparing the uncertainty analysis outcomes of all models.
- Investigate the effect of increasing **reservoir permeability (k) variance** and **depth** on the uncertainty outcomes including optimal heterogeneity resolution(s). At deep depth, investigate **gravity-stable** injection.

Project Overview:

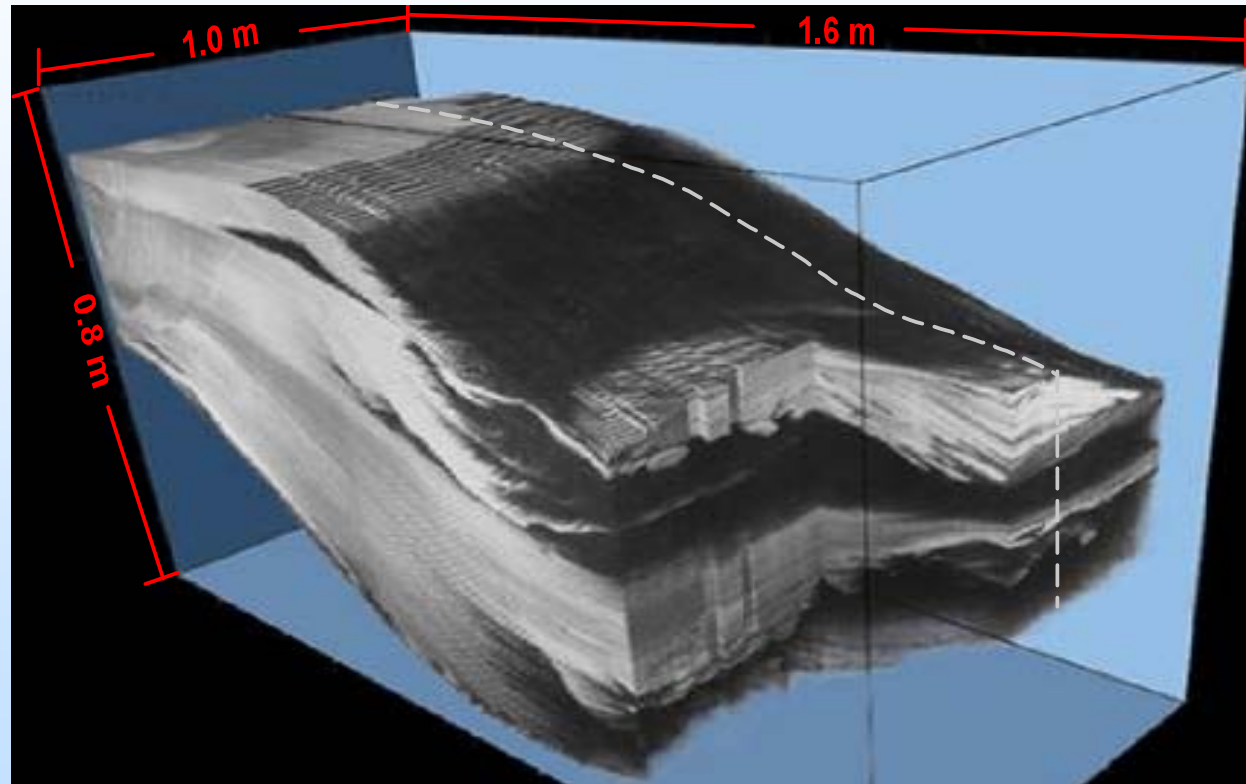
Success Criteria

- At increasing depth, for both weakly and strongly heterogeneous systems, the geologic models can capture the FHM CO₂ behaviors within the full parameter space; → **Reduced characterization cost**;
- RS analytical models are successfully verified against full-physics reservoir simulations via HPC, thus prediction uncertainty of any outcome at any time can be assessed using the low-resolution model(s) running the efficient RS models. → **Enhanced computation efficiency**;
- Deep injection: within the uncertainty analysis framework, identify the combination(s) of favorable parameters & reservoir condition that give rise to gravity stable flow → **Enhanced storage security**.

Accomplishments to Date

- High-resolution 3D reservoir k heterogeneity (3.2 M) & geologic models of **decreasing** k resolutions;
- Permeability upscaling & single-phase flow verification;
- (poster tomorrow) Multiscale dispersivity upscaling & verification via a new parallel RWPT with $\text{div}(D)$;
- CO_2 modeling with PFLOTRAN & performance scaling on the petascale Yellowstone supercomputer at NWSC;
- Preliminary model comparison & DoE/RS analysis.

Sediment Experiment at SAFL



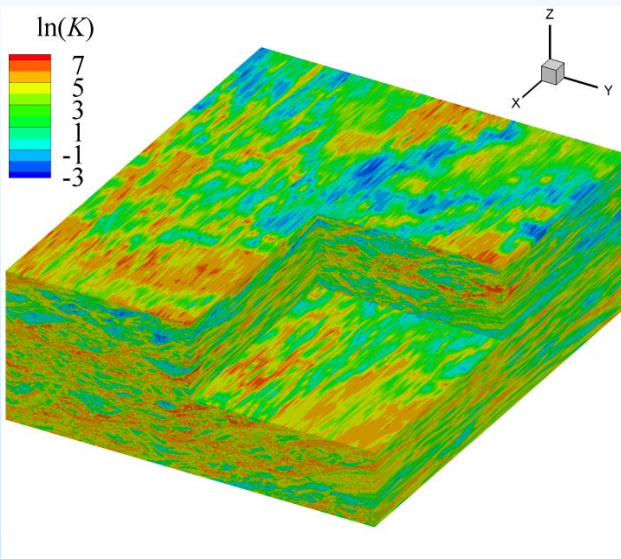
<http://www.safl.umn.edu/>

Project lead: Prof. Chris Paola

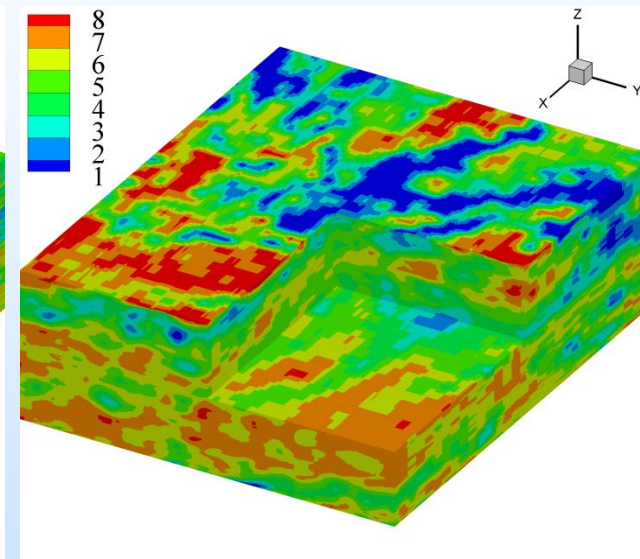
Funding: NSF & oil industry consortium

Reservoir Heterogeneity v. Geologic Models

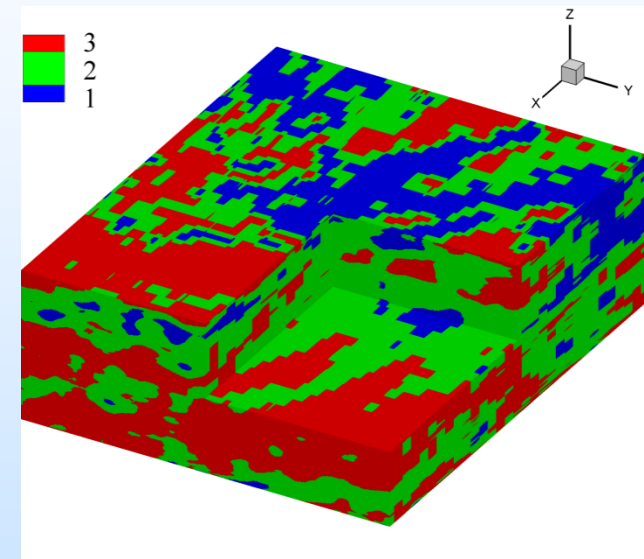
$N_x=251, N_y=251, N_z=50$ (total grid cells = 3.2M)



FHM



8-unit facies model



3-unit facies model

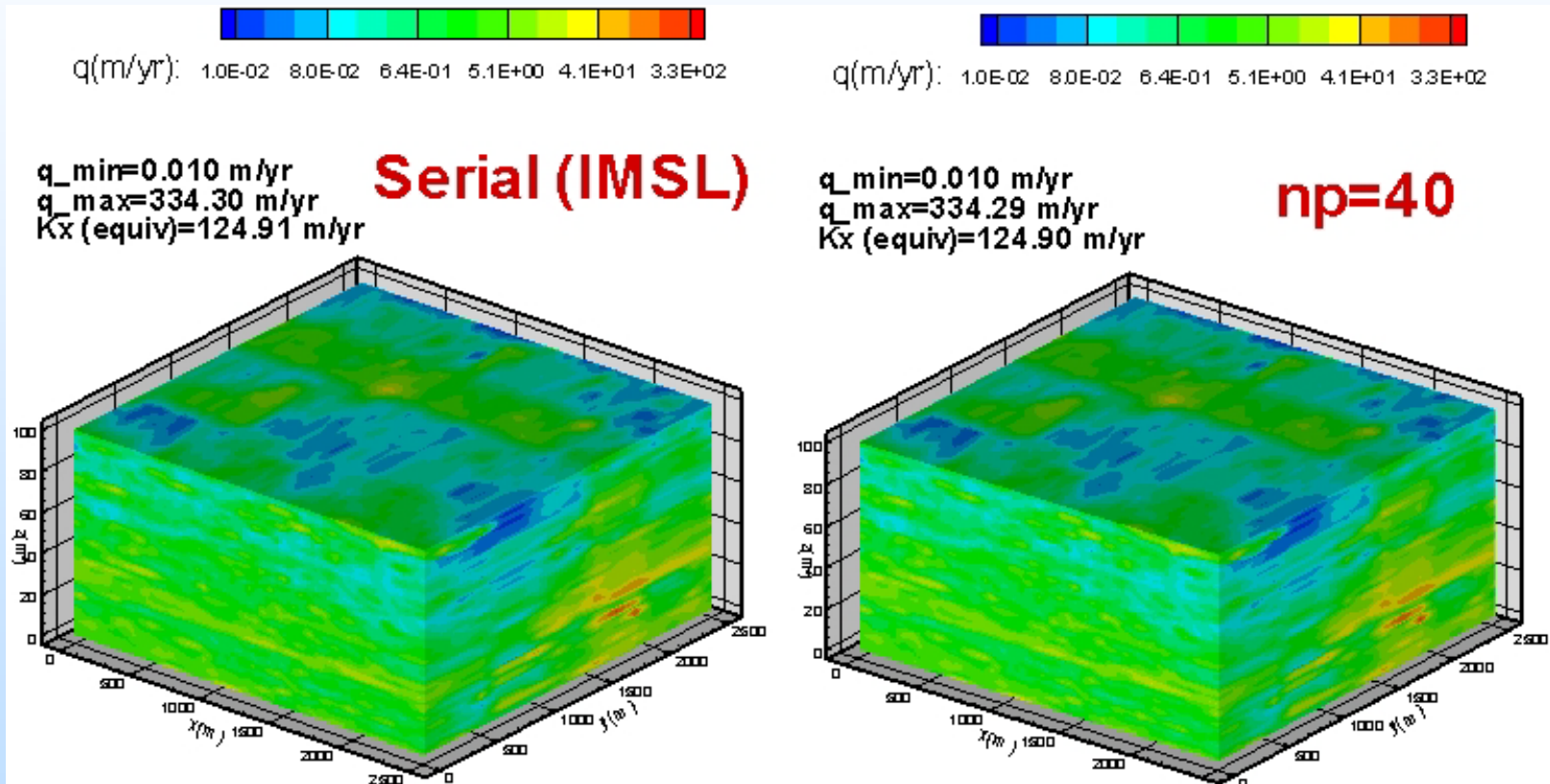
- A 1-unit homogeneous “formation” model is also created (not shown);
- A homogeneous shale caprock unit is added to all models (not shown);

Intrinsic Permeability Upscaling

| | | | | | | | | | | | |
|-----------------|--|--|--|--|--|--|--|--|--|---|-------------------------|
| BC ₁ | $\langle \frac{\partial \Phi}{\partial x} \rangle_1$ | $\langle \frac{\partial \Phi}{\partial y} \rangle_1$ | $\langle \frac{\partial \Phi}{\partial z} \rangle_1$ | 0 | 0 | 0 | 0 | 0 | 0 | $\left. \begin{matrix} k_{xx} \\ k_{xy} \\ k_{xz} \end{matrix} \right\} = (-\mu)$ | $\langle q_x \rangle_1$ |
| | 0 | 0 | 0 | $\langle \frac{\partial \Phi}{\partial x} \rangle_1$ | $\langle \frac{\partial \Phi}{\partial y} \rangle_1$ | $\langle \frac{\partial \Phi}{\partial z} \rangle_1$ | 0 | 0 | 0 | | $\langle q_y \rangle_1$ |
| | 0 | 0 | 0 | 0 | 0 | 0 | $\langle \frac{\partial \Phi}{\partial x} \rangle_1$ | $\langle \frac{\partial \Phi}{\partial y} \rangle_1$ | $\langle \frac{\partial \Phi}{\partial z} \rangle_1$ | | $\langle q_z \rangle_1$ |
| BC ₂ | $\langle \frac{\partial \Phi}{\partial x} \rangle_2$ | $\langle \frac{\partial \Phi}{\partial y} \rangle_2$ | $\langle \frac{\partial \Phi}{\partial z} \rangle_2$ | 0 | 0 | 0 | 0 | 0 | 0 | $\left. \begin{matrix} k_{yx} \\ k_{yz} \end{matrix} \right\}$ | $\langle q_x \rangle_2$ |
| | 0 | 0 | 0 | $\langle \frac{\partial \Phi}{\partial x} \rangle_2$ | $\langle \frac{\partial \Phi}{\partial y} \rangle_2$ | $\langle \frac{\partial \Phi}{\partial z} \rangle_2$ | 0 | 0 | 0 | | $\langle q_y \rangle_2$ |
| | 0 | 0 | 0 | 0 | 0 | 0 | $\langle \frac{\partial \Phi}{\partial x} \rangle_2$ | $\langle \frac{\partial \Phi}{\partial y} \rangle_2$ | $\langle \frac{\partial \Phi}{\partial z} \rangle_2$ | | $\langle q_z \rangle_2$ |
| ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | $\left. \begin{matrix} k_{yy} \end{matrix} \right\}$ | ... |
| BC _m | $\langle \frac{\partial \Phi}{\partial x} \rangle_m$ | $\langle \frac{\partial \Phi}{\partial y} \rangle_m$ | $\langle \frac{\partial \Phi}{\partial z} \rangle_m$ | 0 | 0 | 0 | 0 | 0 | 0 | $\left. \begin{matrix} k_{zx} \\ k_{zy} \end{matrix} \right\}$ | $\langle q_x \rangle_m$ |
| | 0 | 0 | 0 | $\langle \frac{\partial \Phi}{\partial x} \rangle_m$ | $\langle \frac{\partial \Phi}{\partial y} \rangle_m$ | $\langle \frac{\partial \Phi}{\partial z} \rangle_m$ | 0 | 0 | 0 | | $\langle q_y \rangle_m$ |
| | 0 | 0 | 0 | 0 | 0 | 0 | $\langle \frac{\partial \Phi}{\partial x} \rangle_m$ | $\langle \frac{\partial \Phi}{\partial y} \rangle_m$ | $\langle \frac{\partial \Phi}{\partial z} \rangle_m$ | | $\langle q_z \rangle_m$ |
| Symmetry | 0 | 1 | 0 | -1 | 0 | 0 | 0 | 0 | 0 | $\left. \begin{matrix} k_{zz} \end{matrix} \right\}$ Zhang et al. (2006) WRR; Li et al. (2011) WRR | 0 |
| | 0 | 0 | 1 | 0 | 0 | 0 | -1 | 0 | 0 | | 0 |
| | 0 | 1 | 0 | 0 | 0 | 1 | 0 | -1 | 0 | | 0 |

Parallel Flow Simulation for Upscaling

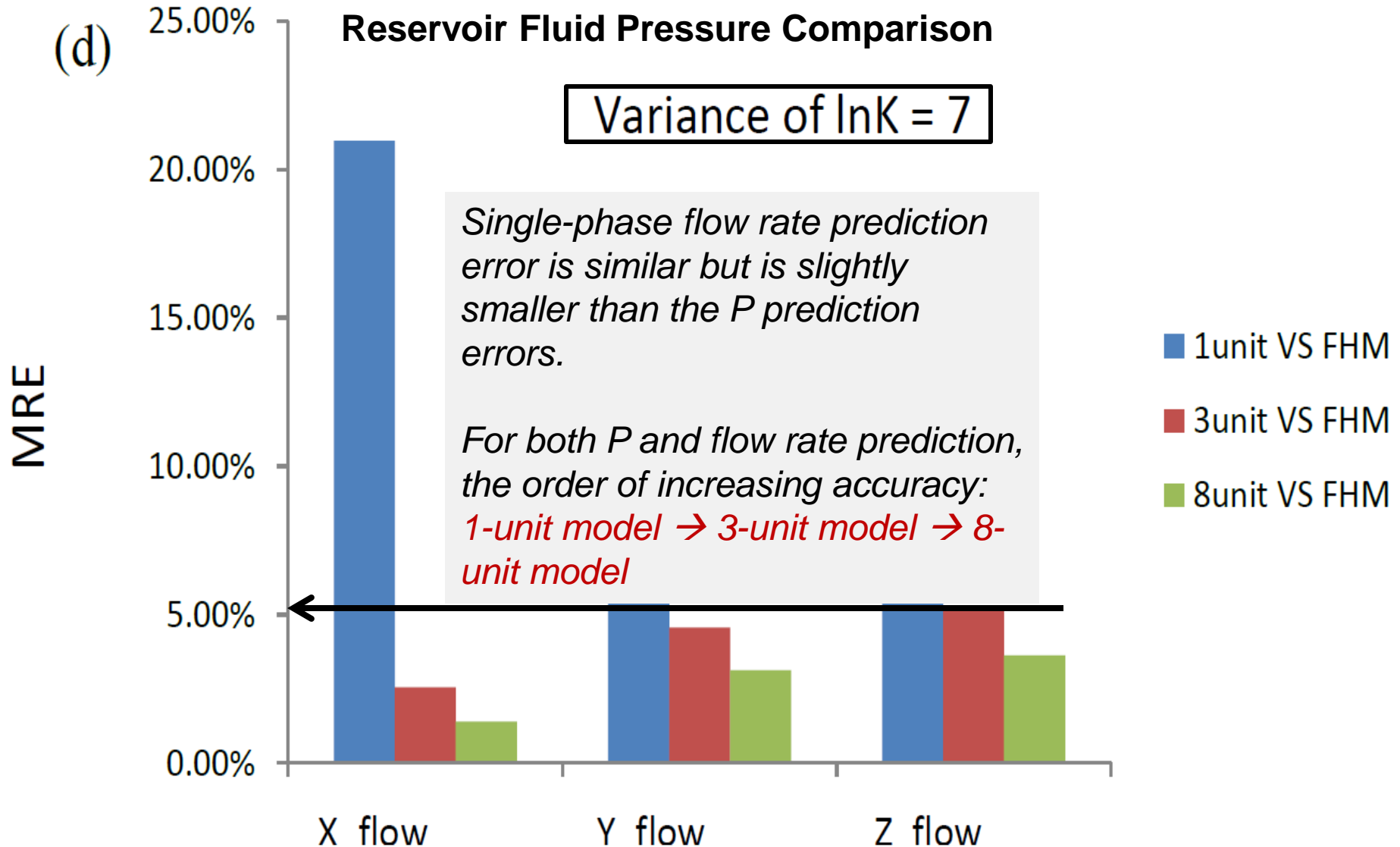
Test model (0.4M):



Serial time (calling an optimized IMSL on BigRed at IU):
Parallel time (H2oc.gg.uwyo.edu):

1 hour
37 sec (64 processors)

Upscaling Verification



Upscaling Summary

- Global upscaling can homogenize irregularly shaped & hierarchical geologic models with reservoir-scale (long-range) k connectivity;
- Upscaling is successful even for high-variance systems (the highest successfully tested reservoir k varies $\sim 10^6$);
- Parallel HPC can overcome the computational hurdle associated with the global upscaling of large models;
- (poster tomorrow) A dispersivity upscaling analysis is conducted to estimate the effective longitudinal macrodispersivity for each unit of the geologic models, for both the low and high *lnk* variance systems.

CO₂ Modeling with PFLOTRAN

- Multicomponent-multiphase-multiphysics non-isothermal reactive flow and transport model;
- Massively parallel---based on the PETSc parallel framework;
 - Peta-scale performance
 - Highly scalable (run on over 265k cores)
- Supercritical CO₂-H₂O
 - Span-Wagner EOS for CO₂ density & fugacity coefficient
 - Mixture density for dissolved CO₂-brine (Duan et al., 2008)
 - Viscosity CO₂ (Fenghour et al., 1998)
- Finite Volume Discretization
 - Variable switching for changes in fluid phase
 - Structured/Unstructured grids
- Object Oriented Fortran 2003
 - Open Source (Multilab code: LANL, LBNL, ORNL, PNNL)

PFLOTRAN Scaling on Yellowstone

Yellowstone is a 1.5-petaflops supercomputer with 72,288 processor cores & 144.6 TB of memory.

<http://www2.cisl.ucar.edu/resource/s/yellowstone>

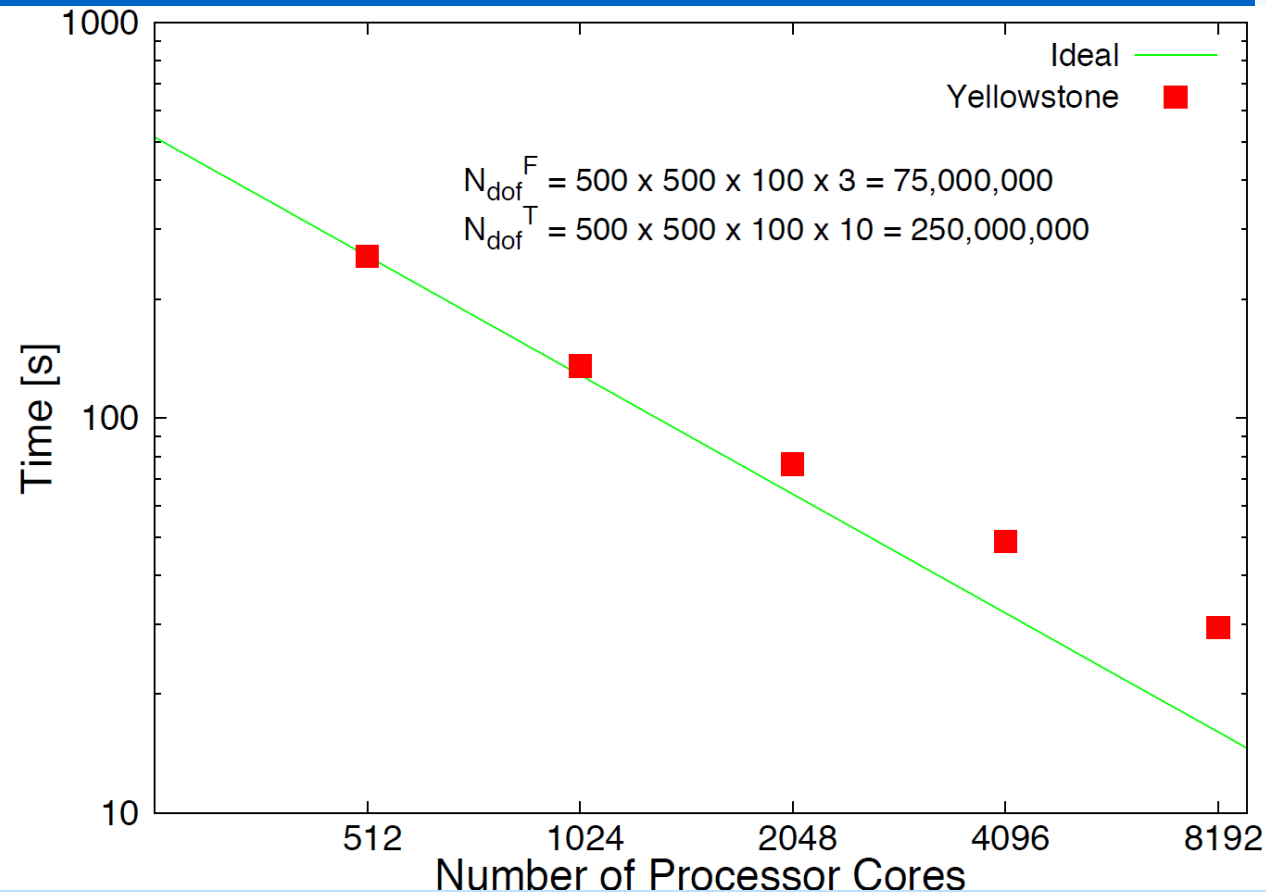
We can solve bigger problems, but we cannot access all these cores at all times!

1-unit model (3.2M):

* 20 yr CO₂ injection + 1000 yr monitoring

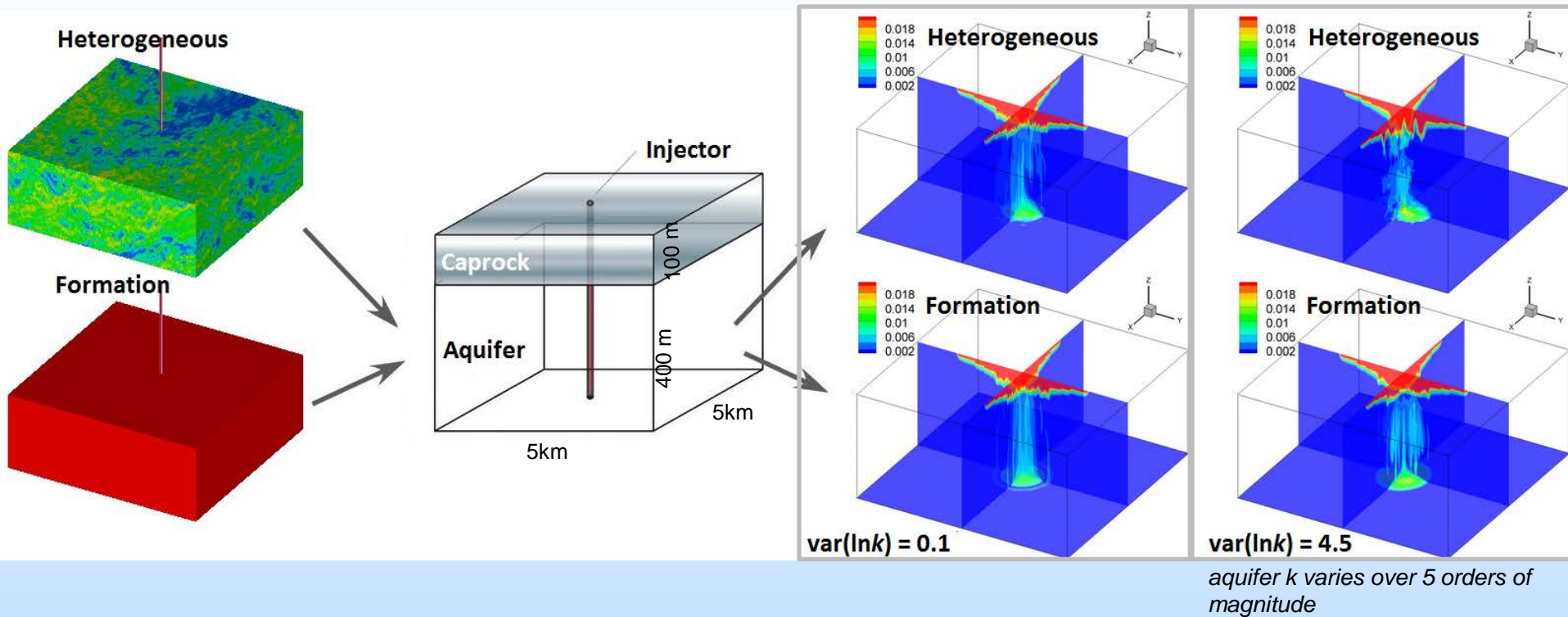
* **1024 cores:** 5 min = 2 min (injection) + 3 min (monitoring)

1-unit model (25 M): CO₂ injection w/ reactive chemistry



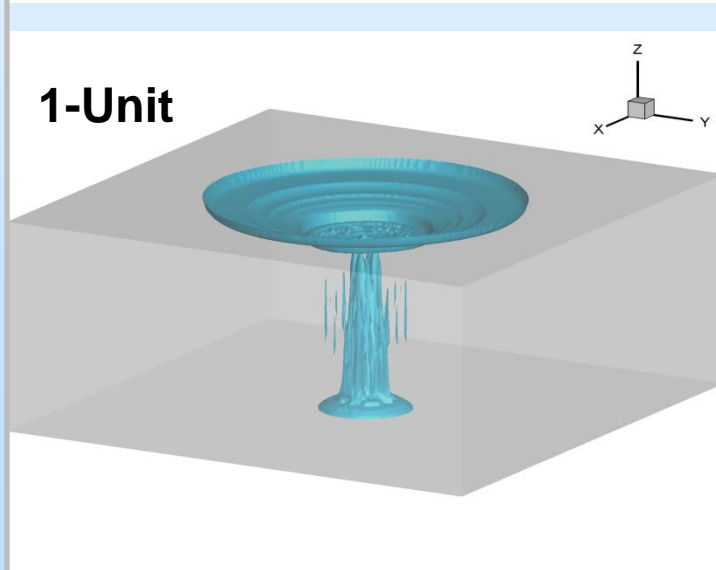
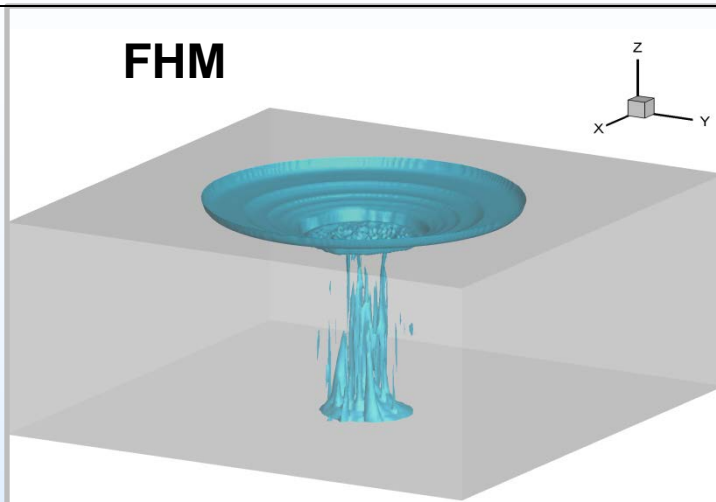
CO₂ Simulation: FHM v. 1-Unit Model

Dissolved CO₂ at the end of monitoring (inj rate= 0.05 Mt/yr):

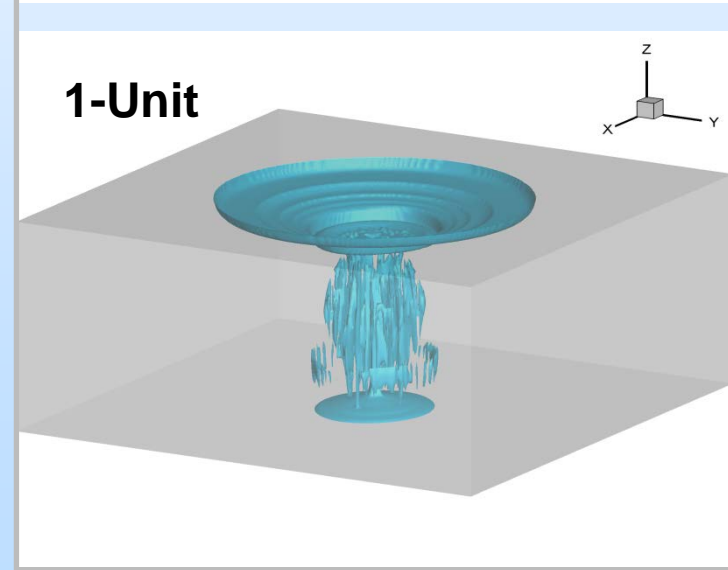
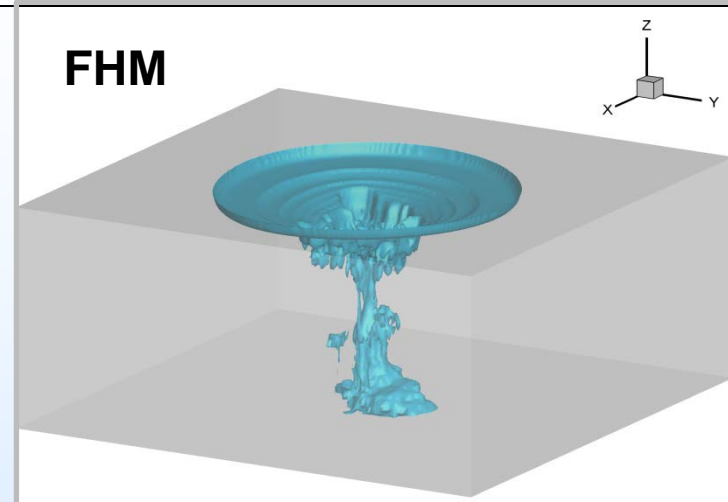


- Under **both** low and high variance conditions, the 1-unit model can capture the plume footprint (see above) and fluid pressure (Appendix) of the FHM very well.
- Based on results of the upscaling study, the 8-unit and 3-unit models should yield more accurate CO₂ predictions than the 1-unit model → **yet to be simulated**.

End of Monitoring: Iso_conc = 0.004

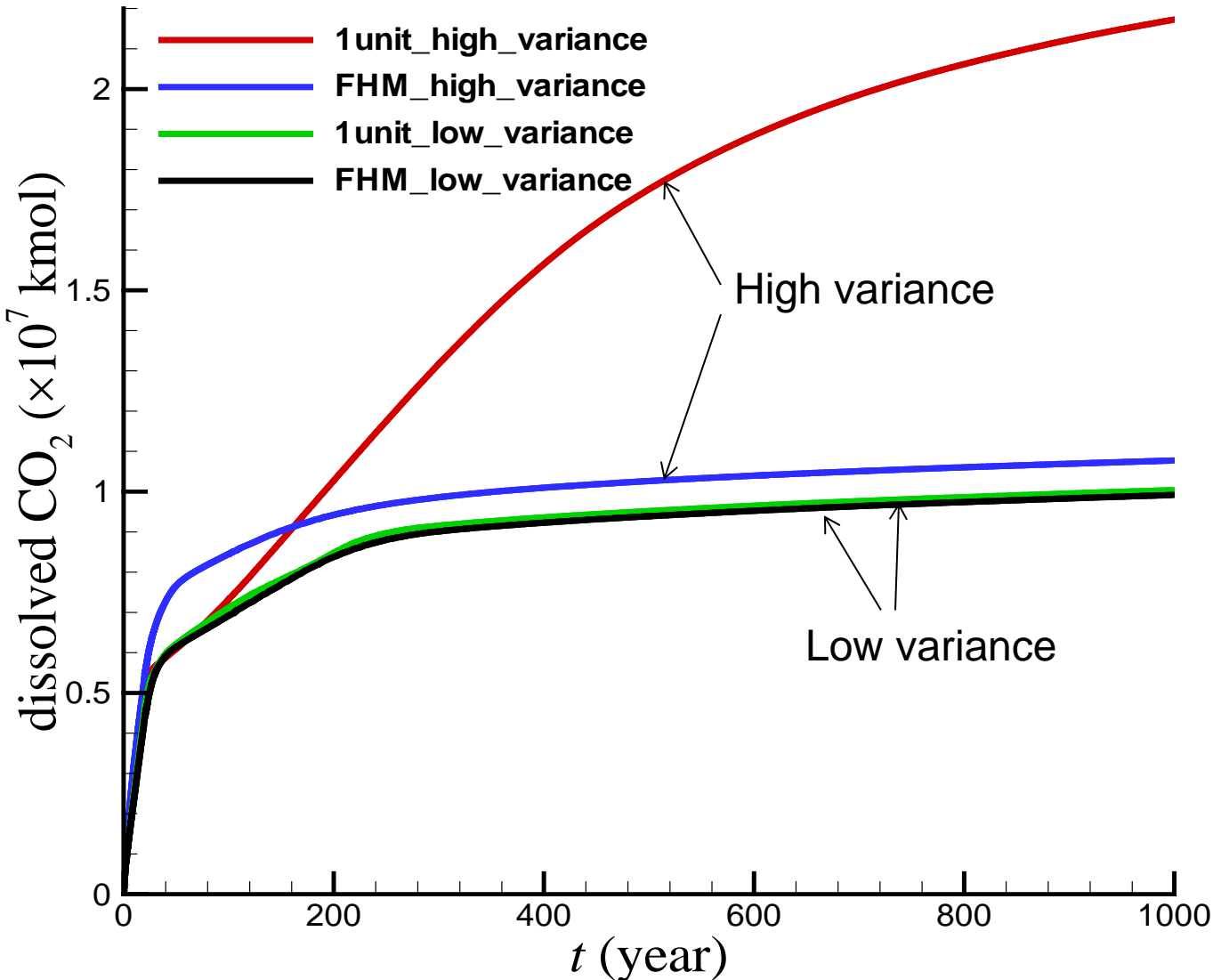


Var(Ink)=0.1



Var(Ink)=4.5

FHM v. 1-Unit Model: Dissolved CO₂



- Under low variance, the 1-unit model can capture the dissolved CO₂ well;
- Under high variance, the 1-unit model over-estimates the dissolved CO₂ because the equivalent k_z is high → **faster density-driven convection** → more CO₂ dissolved per unit time;
- Under high variance, how accurate are the 8-unit and 3-unit models remain to be seen.

Design of Experiment: 1-Unit

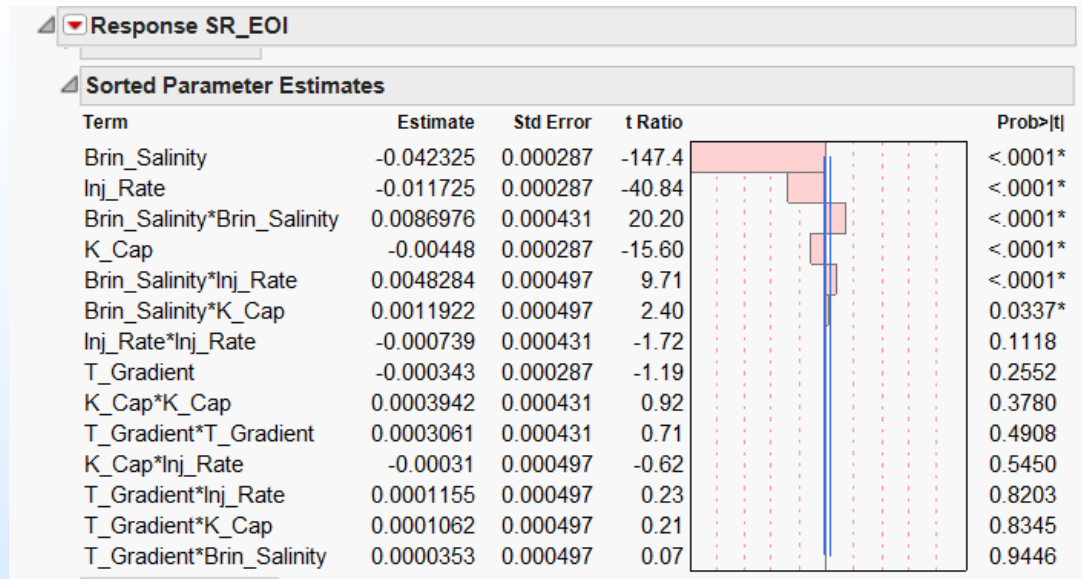
| | Pattern | T_Gradient | Brin_Salinity | K_Cap | Inj_Rate | SR_EOI | SR_EOM | CO2_LK_EOI | CO2_LK_EOM | Brin_LK_EOI | Brin_LK_EOM |
|----|---------|------------|---------------|-------|----------|-------------|-------------|------------|-------------|--------------|-------------|
| 1 | ++00 | 1 | 1 | 0 | 0 | 0.10835058 | 0.296383093 | 2.45e-12 | 1.31e-10 | 0.0000000678 | 0.00000361 |
| 2 | 0+0- | 0 | 1 | 0 | -1 | 0.115352993 | 0.290742974 | 3.99e-12 | 9.84e-11 | 0.00000011 | 0.00000272 |
| 3 | 0000 | 0 | 0 | 0 | 0 | 0.142377741 | 0.538398262 | 1.7e-12 | 9.23e-11 | 0.0000000466 | 0.00000253 |
| 4 | -00- | -1 | 0 | 0 | -1 | 0.153843493 | 0.55349839 | 2.48e-12 | 6.18e-11 | 0.0000000678 | 0.00000169 |
| 5 | 0--0 | 0 | -1 | -1 | 0 | 0.199386363 | 0.437694529 | 2.13e-11 | 9.38e-10 | 0.000000583 | 0.00000256 |
| 6 | 0+0+ | 0 | 1 | 0 | 1 | 0.100143073 | 0.284811298 | 7.88e-13 | 9.84e-11 | 0.0000000218 | 0.00000272 |
| 7 | -0+0 | -1 | 0 | 1 | 0 | 0.138510286 | 0.687346742 | -1.77e-13 | 5.09e-12 | -4.84e-9 | 0.000000139 |
| 8 | --00 | -1 | -1 | 0 | 0 | 0.19363702 | 0.795624274 | 1.11e-12 | 6.17e-11 | 0.0000000302 | 0.00000168 |
| 9 | +00- | 1 | 0 | 0 | -1 | 0.152782269 | 0.552892793 | 4.92e-12 | 1.22e-10 | 0.000000135 | 0.00000336 |
| 10 | +0+0 | 1 | 0 | 1 | 0 | 0.138169204 | 0.672851482 | -3.45e-13 | 1.01e-11 | -9.48e-9 | 0.000000276 |
| 11 | 0--0 | 0 | -1 | 1 | 0 | 0.187461554 | 0.930414357 | -2.96e-13 | 7.44e-12 | -8.08e-9 | 0.000000203 |
| 12 | +0-0 | 1 | 0 | -1 | 0 | 0.147983085 | 0.297567526 | 2.84e-11 | 1.25e-9 | 0.000000078 | 0.00000342 |
| 13 | +00+ | 1 | 0 | 0 | 1 | 0.13057312 | 0.514362598 | 9.6e-13 | 1.22e-10 | 0.0000000264 | 0.00000336 |
| 14 | 00+- | 0 | 0 | 1 | -1 | 0.149784337 | 0.703780661 | -2.01e-13 | 7.59e-12 | -5.52e-9 | 0.000000208 |
| 15 | 0+-0 | 0 | 1 | -1 | 0 | 0.113389545 | 0.221478542 | 2.28e-11 | 0.000000001 | 0.000000631 | 0.00000276 |
| 16 | 0000 | 0 | 0 | 0 | 0 | 0.142377741 | 0.538398262 | 1.7e-12 | 9.23e-11 | 0.0000000466 | 0.00000253 |
| 17 | 00-- | 0 | 0 | 1 | -1 | 0.156476955 | 0.282904316 | 4.28e-11 | 9.39e-10 | 0.00000117 | 0.00000257 |
| 18 | +--00 | 0 | 0 | 0 | 0 | 0.192891704 | 0.787607997 | 2.21e-12 | 1.22e-10 | 0.0000000606 | 0.00000334 |
| 19 | 00+- | 0 | 0 | 1 | 1 | 0.134054747 | 0.306602194 | 1.05e-11 | 9.39e-10 | 0.000000288 | 0.00000257 |
| 20 | 00++ | 0 | 0 | 1 | 1 | 0.126123131 | 0.665760497 | -2.57e-13 | 7.59e-12 | -7.04e-9 | 0.000000208 |
| 21 | 0-0+ | 0 | 0 | 1 | 1 | 0.176212246 | 0.794850016 | 6.9e-13 | 9.2e-11 | 0.0000000189 | 0.00000251 |
| 22 | --+00 | 0 | 0 | 0 | 0 | 0.108954684 | 0.28941944 | 1.22e-12 | 6.59e-11 | 0.0000000338 | 0.00000182 |
| 23 | -00+ | 0 | 0 | 1 | 1 | 0.131172432 | 0.515158456 | 4.69e-13 | 6.18e-11 | 0.0000000128 | 0.00000169 |
| 24 | -0-0 | -1 | 0 | -1 | 0 | 0.148748884 | 0.296929128 | 1.42e-11 | 6.29e-10 | 0.000000389 | 0.00000172 |
| 25 | 0++0 | 0 | 1 | 1 | 0 | 0.106233377 | 0.319291597 | -2.51e-13 | 8.19e-12 | -6.94e-9 | 0.000000226 |
| 26 | 0000 | 0 | 0 | 0 | 0 | 0.142377741 | 0.538398262 | 1.7e-12 | 9.23e-11 | 0.0000000466 | 0.00000253 |
| 27 | 0-0- | 0 | -1 | 0 | -1 | 0.210735883 | 0.815954164 | 3.66e-12 | 9.2e-11 | 0.0000000999 | 0.00000251 |

Total amount of CO₂ injected is the same among all simulations.

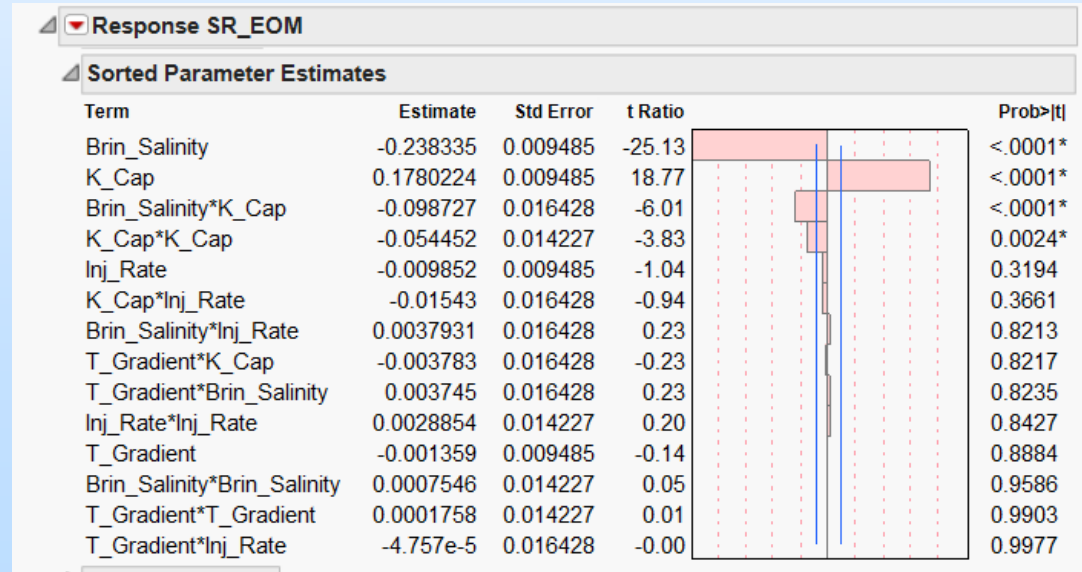
Parameter Ranking: 1-Unit

Outcome:
dissolved CO₂

End of
Injection



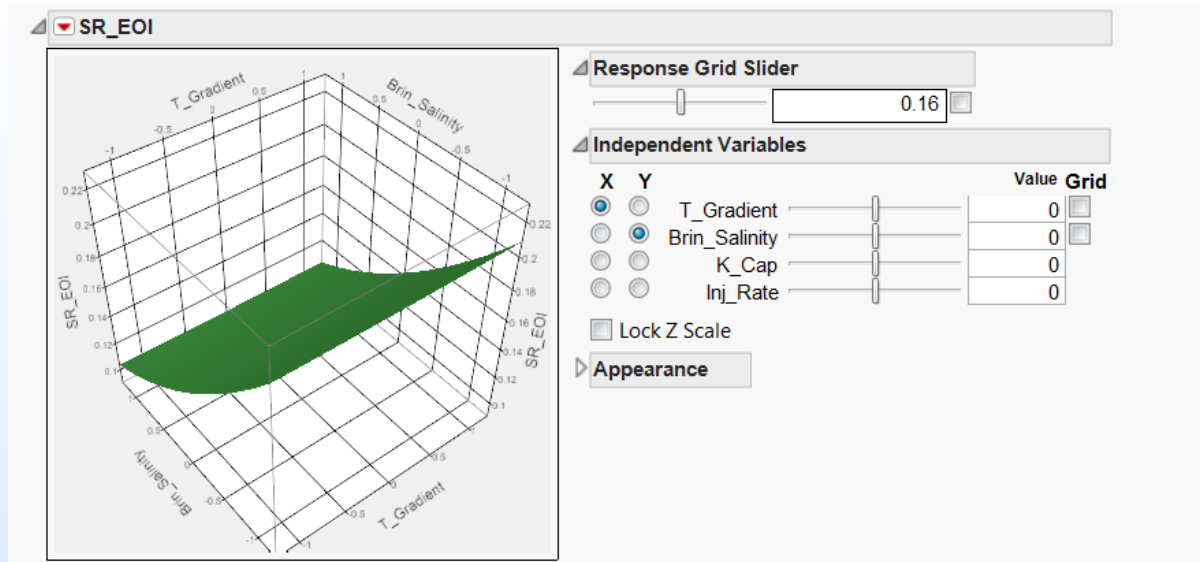
End of
Monitoring



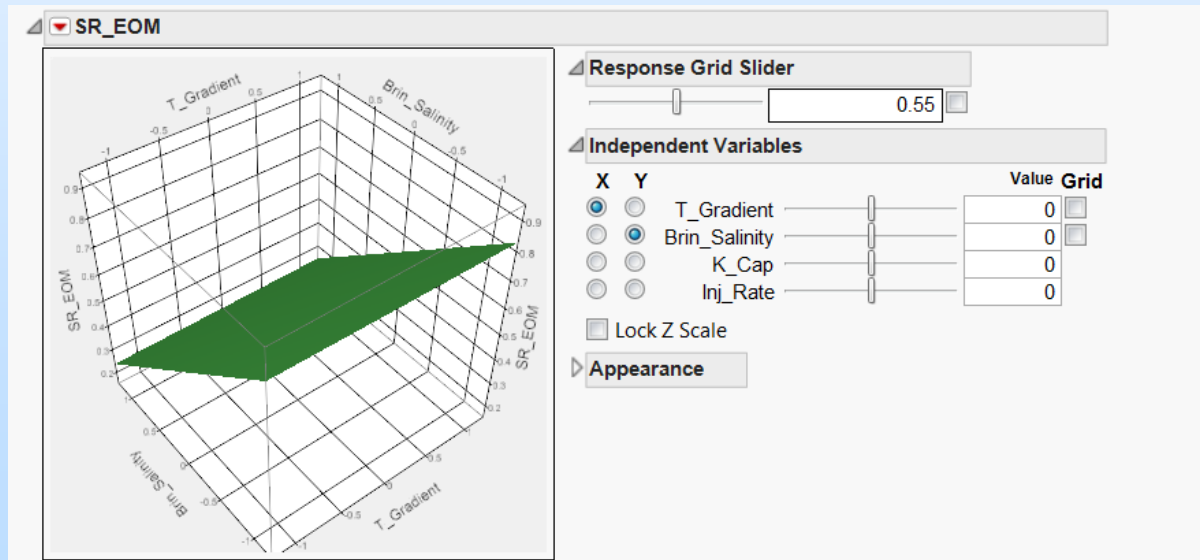
Response Surfaces: 1-Unit

Outcome:
dissolved CO₂

End of
Injection



End of
Monitoring



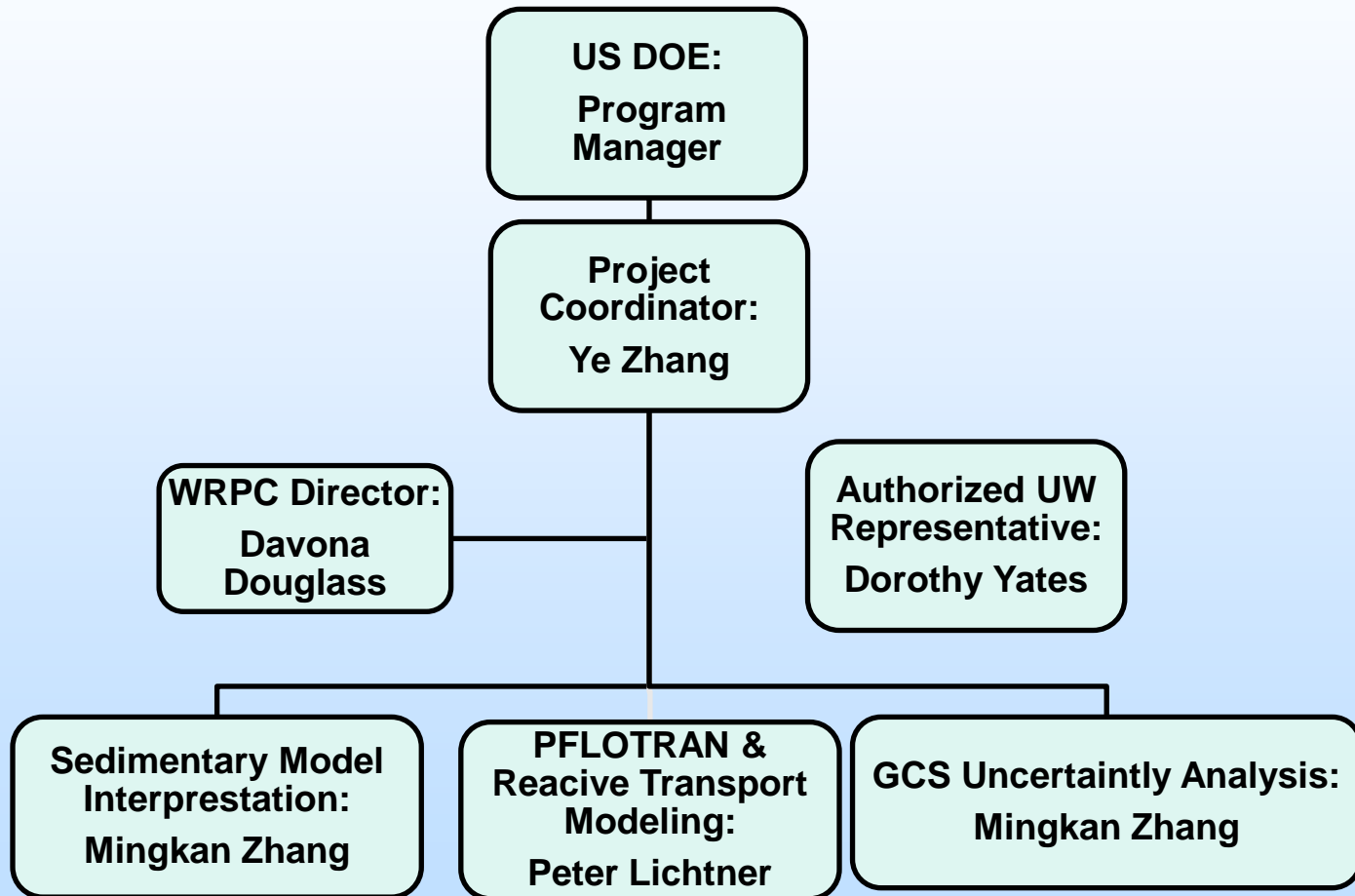
Summary

- Global upscaling computes equivalent k_s for the geologic model with decreasing heterogeneity resolution; for increasing reservoir $\ln k$ variances (0.1, 1.0, 4.5), FHM pressure and flow rate are captured well by the geologic models, but errors increase with variance.
- (poster) Upscaled dispersivities for the 8-, 3-, and 1-unit models can capture plume moments (centroid, longitudinal plume covariance, BTC) when variance is low to modest.
- When the variance of $\ln(k)$ is low, the 1-unit model yields very similar reservoir fluid pressure, plume footprint, and dissolution fingering as the FHM. It thus accurately predicts the total dissolution storage at the end of the simulation time.
- When the variance of $\ln(k)$ is high, the 1-unit model yields similar reservoir fluid pressure (slight increase in error) and plume footprint as the FHM, but predicts more dissolution fingering per unit time (more optimistic storage estimate).
- Preliminary experimental design analysis suggests that brine salinity is the single most influential factor impacting CO_2 dissolution storage in the 1-unit model.
- **Next step: For low and high variance systems, complete the DoE and RS analysis for all models to compare their parameter sensitivity & prediction uncertainty.**

Appendix

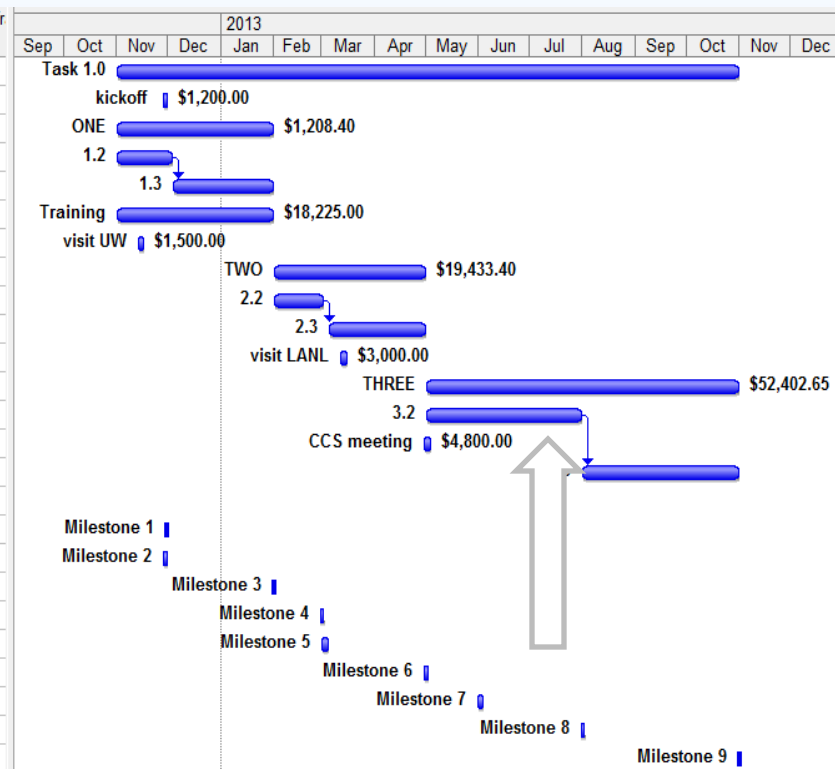
- These slides will not be discussed during the presentation, **but are mandatory**

Organization Chart



Gantt Chart: Budget Period 1

| Budget Period 1 | Task Name | Duration | Start | Finish | Travel | PI+Co-PI | Postdoc+UC | Personnel+Tr |
|-----------------|---|----------|--------------|--------------|------------|-------------|-------------|--------------|
| Task 1.0 | PMP | 261 days | Thu 11/1/12 | Thu 10/31/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| kickoff | Project kickoff meeting | 3 days | Wed 11/28/12 | Fri 11/30/12 | \$1,200.00 | \$0.00 | \$0.00 | \$1,200.00 |
| ONE | Creation of Hierarchical Models | 66 days | Thu 11/1/12 | Thu 1/31/13 | \$0.00 | \$0.00 | \$1,208.40 | \$1,208.40 |
| 1.2 | Lithofacies mapping in 3D | 23 days | Thu 11/1/12 | Mon 12/3/12 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| 1.3 | Create stratigraphic models of decreasing | 43 days | Tue 12/4/12 | Thu 1/31/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| Training | Training of postdoc in techniques & HPC | 66 days | Thu 11/1/12 | Thu 1/31/13 | \$0.00 | \$0.00 | \$18,225.00 | \$18,225.00 |
| visit UW | Co-PI visit UW | 4 days? | Tue 11/13/12 | Fri 11/16/12 | \$1,500.00 | \$0.00 | \$0.00 | \$1,500.00 |
| TWO | Permeability Upscaling & Verification | 63 days | Fri 2/1/13 | Tue 4/30/13 | \$0.00 | \$0.00 | \$19,433.40 | \$19,433.40 |
| 2.2 | Calculate 3D equivalent permeability | 21 days | Fri 2/1/13 | Fri 3/1/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| 2.3 | Verify the equivalent permeability | 41 days | Tue 3/5/13 | Tue 4/30/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| visit LANL | PI & postdoc visiting Co-PI | 4 days? | Tue 3/12/13 | Fri 3/15/13 | \$3,000.00 | \$0.00 | \$0.00 | \$3,000.00 |
| THREE | Uncertainty Analysis -- Non-reactive geoc | 132 days | Wed 5/1/13 | Thu 10/31/13 | \$0.00 | \$15,952.65 | \$36,450.00 | \$52,402.65 |
| 3.2 | Conduct a screening DoE analysis | 66 days | Wed 5/1/13 | Wed 7/31/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| CCS meeting | Project Team attend annual CCS | 4 days | Tue 4/30/13 | Fri 5/3/13 | \$4,800.00 | \$0.00 | \$0.00 | \$4,800.00 |
| 3.3 | Conduct a RS analysis, verification, MC | 66 days | Thu 8/1/13 | Thu 10/31/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| Milestone 1 | Updated PMP | 2 days | Thu 11/29/12 | Fri 11/30/12 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| Milestone 2 | Kickoff Meeting | 3 days | Wed 11/28/12 | Fri 11/30/12 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| Milestone 3 | Completion of Task ONE 1.2, 1.3 | 2 days | Thu 1/31/13 | Fri 2/1/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| Milestone 4 | Updated PMP | 2 days | Thu 2/28/13 | Fri 3/1/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| Milestone 5 | Completion of Task TWO 2.2 | 2 days | Fri 3/1/13 | Mon 3/4/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| Milestone 6 | Completion of Task TWO 2.3 | 3 days | Tue 4/30/13 | Thu 5/2/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| Milestone 7 | Updated PMP | 2 days | Fri 5/31/13 | Mon 6/3/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| Milestone 8 | Completion of Task THREE 3.2 | 2 days | Wed 7/31/13 | Thu 8/1/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |
| Milestone 9 | Completion of Task THREE 3.3 | 2 days | Thu 10/31/13 | Fri 11/1/13 | \$0.00 | \$0.00 | \$0.00 | \$0.00 |



PFLOTRAN formulations

To model GCS, the following mass and energy conservation equations are solved:

$$\frac{\partial}{\partial t} \left[\varphi \sum_{\alpha} (\rho_{\alpha} s_{\alpha} X_i^{\alpha}) \right] + \nabla \cdot \sum_{\alpha} (\rho_{\alpha} X_i^{\alpha} \vec{q}_{\alpha} - \varphi \rho_{\alpha} s_{\alpha} \tau_{\alpha} D_{\alpha} \nabla X_i^{\alpha}) = S_i \quad (1)$$

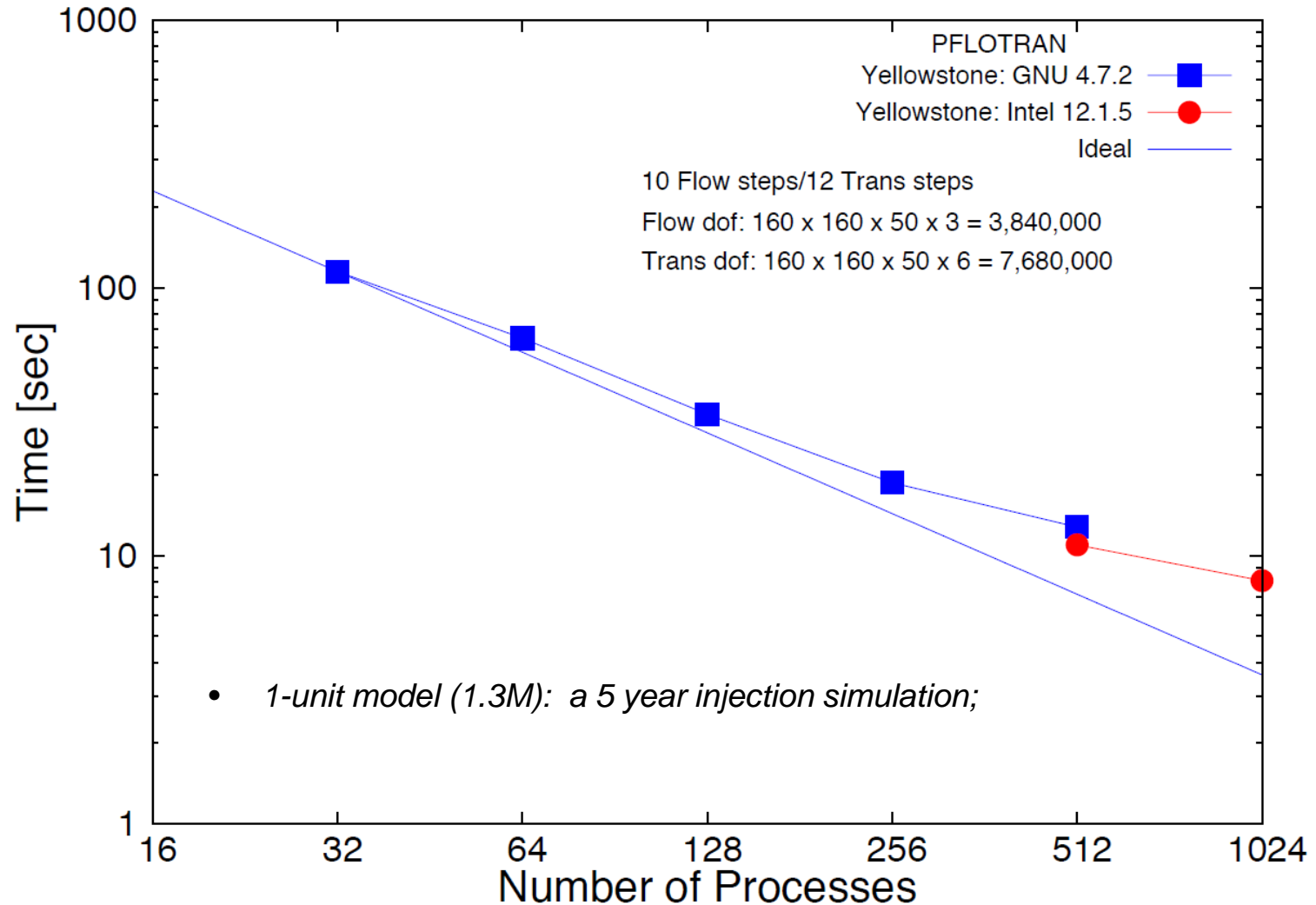
$$\frac{\partial}{\partial t} \left[\varphi \sum_{\alpha} (\rho_{\alpha} s_{\alpha} U_{\alpha}) + (1 - \varphi) \rho_r C_{p,r} T \right] + \nabla \cdot \left[\sum_{\alpha} (\vec{q}_{\alpha} \rho_{\alpha} H_{\alpha}) - \lambda \nabla T \right] = Q \quad (2)$$

φ denotes porosity, and $\rho_{\alpha}, s_{\alpha}, \tau_{\alpha}, D_{\alpha}, U_{\alpha}, H_{\alpha}$ refer to the density, saturation, tortuosity, diffusion coefficient, internal energy, and enthalpy of fluid phase α , respectively. Two fluid phases (CO₂, brine) will be modeled. The quantities X_i^{α} denote the mole fraction of component i in phase α . The quantities $C_{p,r}$ and λ denote the rock heat capacity and conductivity, respectively. The summation is carried out over all fluid phases present in the system. The system is assumed locally to be in thermodynamic equilibrium with temperature $T(\vec{x}; t)$ at position \vec{x} and time t . The quantity Q denotes an energy source/sink term.

The quantity S_i denotes a source/sink term for the i th primary species describing reaction with minerals given by $S_i = -\sum_m \nu_{im} I_m$, with stoichiometric reaction coefficients ν_{im} and kinetic rate I_m for the m th mineral, taken as positive for precipitation and negative for dissolution.

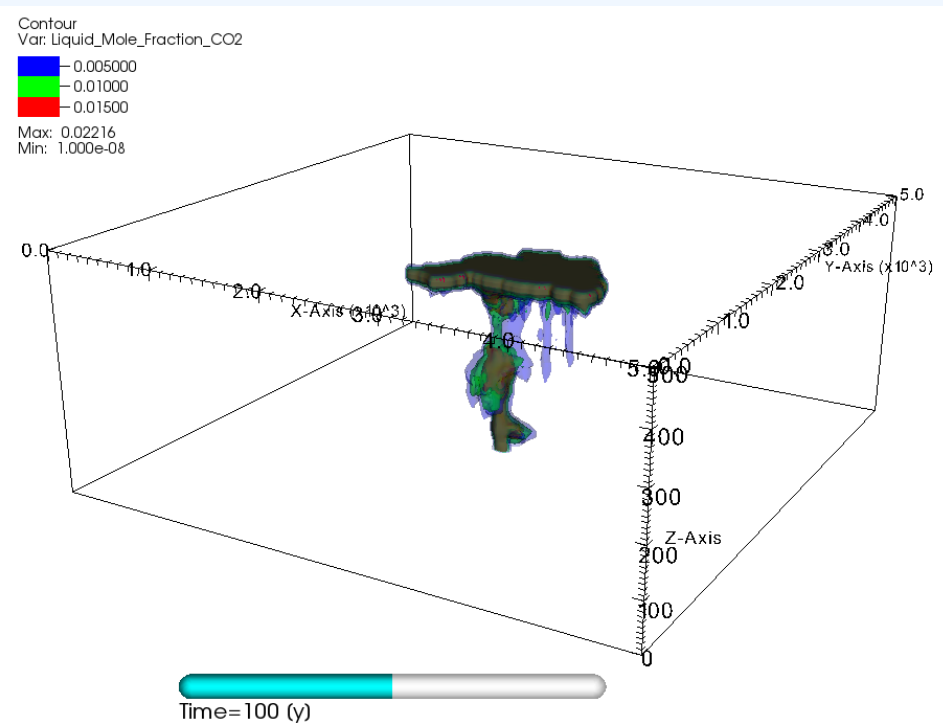
The flow rate \vec{q}_{α} of fluid phase α is given by the extended Darcy's law: $\vec{q}_{\alpha} = -\frac{\bar{k} k_{\alpha}}{\mu_{\alpha}} (\nabla p_{\alpha} - \rho_{\alpha} g z)$, with intrinsic permeability \bar{k} , relative permeability k_{α} , fluid viscosity μ_{α} , and pressure p_{α} of phase α .

PFLOTRAN Scaling on Yellowstone

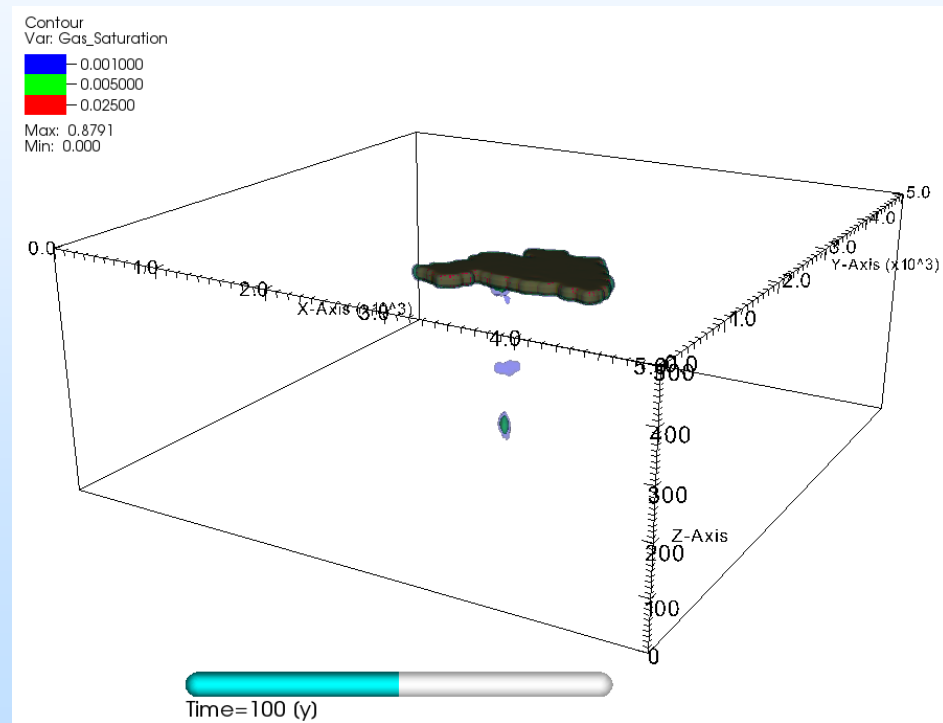


CO₂ Simulation: FHM (Var[lnk]=4.5)

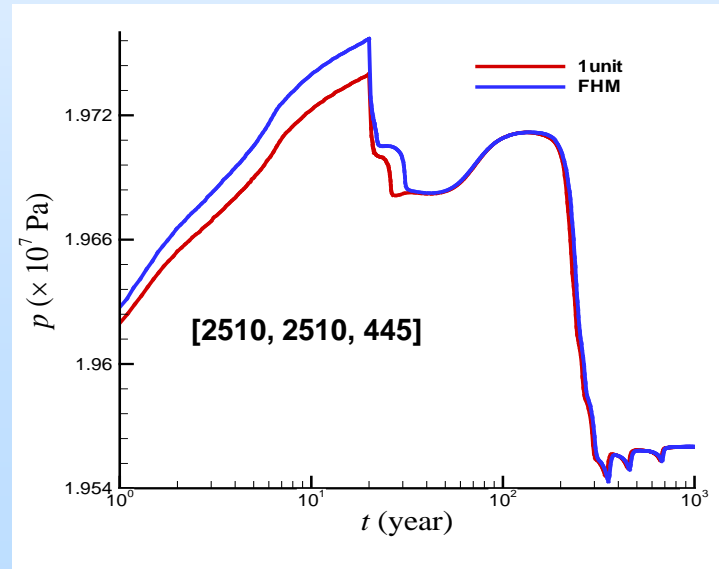
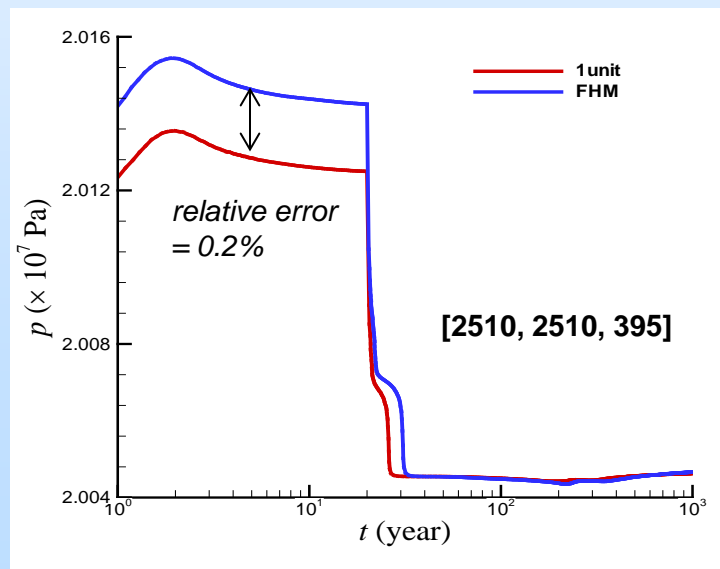
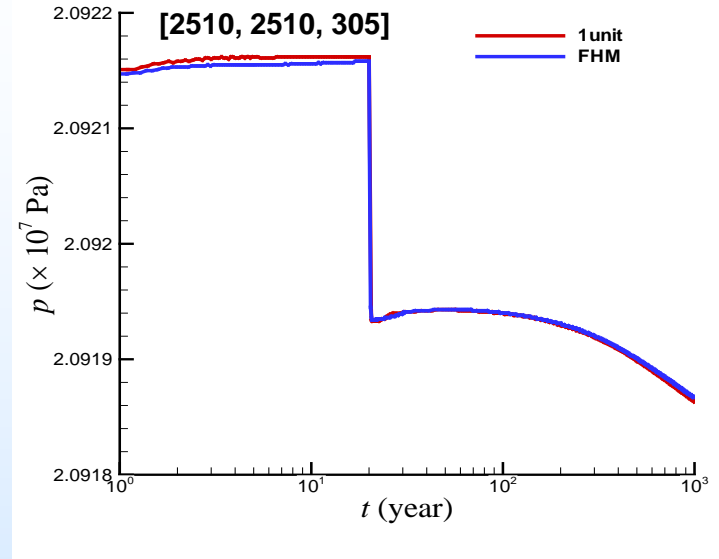
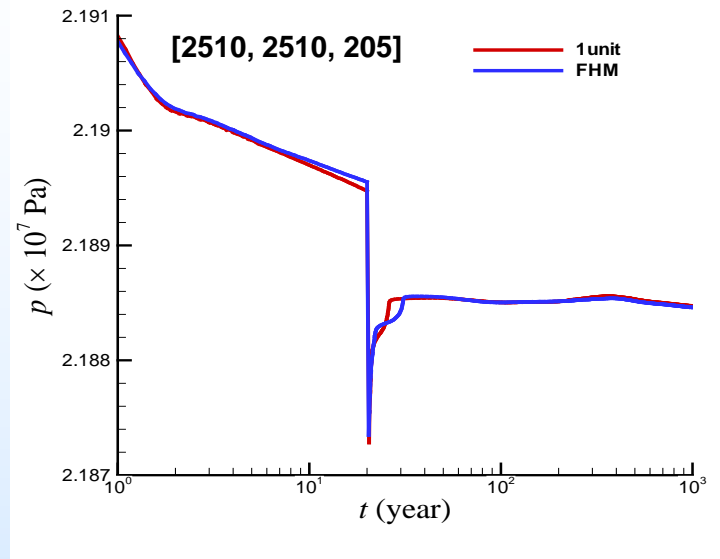
Dissolved CO₂



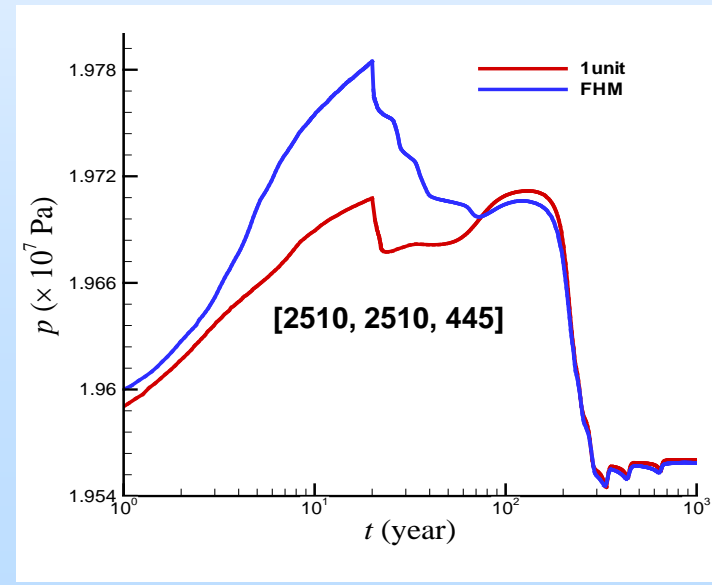
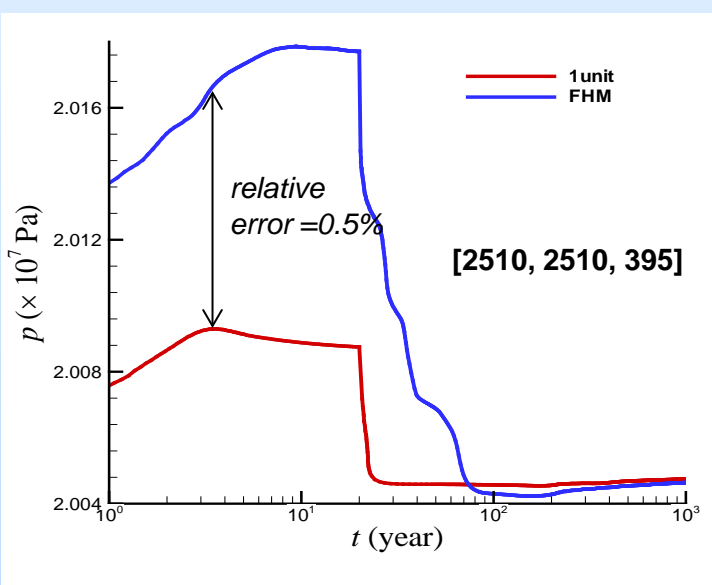
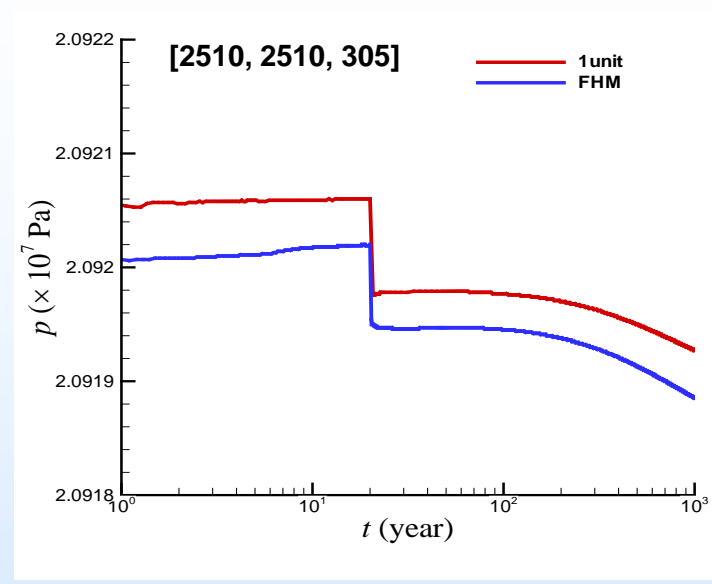
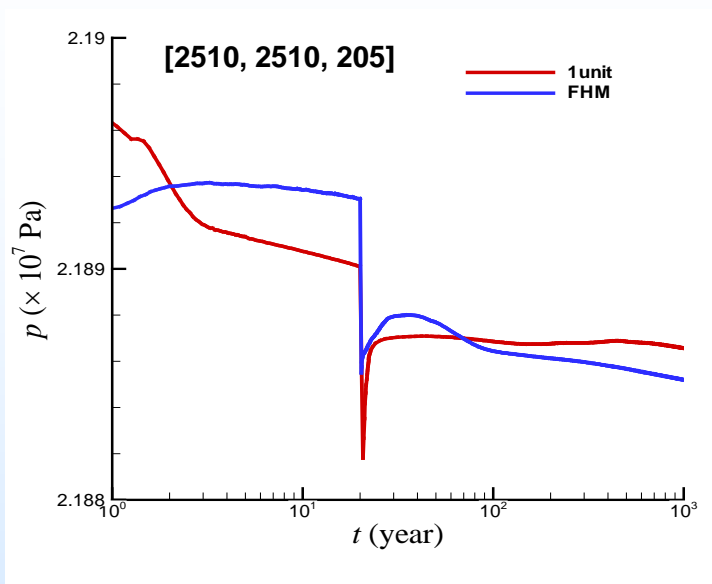
scCO₂



FHM v. 1-Unit Model: $\sigma^2_{\ln k}=0.1$



FHM v. 1-Unit Model: $\sigma^2_{\ln k} = 4.5$



Potential Causes for Delay

CISL Daily Bulletin - August 19, 2013:

Yellowstone InfiniBand recabling set to start Monday, September 30

CISL, IBM, and Mellanox have set Monday, September 30, as the start date for the process of replacing the Yellowstone InfiniBand cables, [previously announced in July](#). Users should plan for Yellowstone being out of service for up to **three weeks** from that date.